

**Referee's report on  
"Study of characteristics of CUSUM-procedure in the change point  
problem"**

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The main purpose of the paper is to derive upper and lower bounds for probabilities that a random walk leaves an interval of fixed width through upper (or lower) boundary point. Such estimates can be used to study error probabilities in the change point problem.

I think that the paper can be of interest for specialists in statistics and deserves to be published in SIMR.

**Major remarks:**

- All obtained bounds seem to be consequences of already known in the literature estimates. This fact does not make them less important, but I would prefer to call the results 'Propositions', not 'Theorems'.
- At two places in the paper, the authors refer to mysterious 'results of computer analysis' without giving any concrete results of simulations. This looks really strange, in particular for a paper with emphasis on applications. There are two options: either the authors remove that sentences or they provide concrete results (e.g. tables) of simulations.
- The bound obtained in the paper do depend on the truncation levels  $c_1$  and  $c_2$ . These two parameters, are chosen to be bigger than  $b$  and  $b$ , in its turn, should be chosen quite large. This implies that the bounds obtained in the paper depend in highly non-trivial way on  $b$ . This can be seen by looking at the definition of the Cramer parameter  $\mu$  on page 6; the value of  $\mu$  depends on  $c_1$ . Consequently,  $c_1$  affects the lower and upper bound on  $Q(x)$ , which are crucial for the strategy in the paper. Because of that, it is very important, to derive bound for  $\mu$  in terms of the truncation level. That would improve the quality of the paper. But I am not insisting on that point, since the implementation can be rather difficult.

**Minor remarks:**

- page 2, line 12:  $\mathbf{E}_1$  is not defined;
- page 4, line 3: I would rearrange a bit the proof of Lemma. I would start by observing that the trajectories of walks  $S$  and  $S'$  coincide before the stopping time  $N$ . Then one can immediately infer that  $N = N'$  and that  $\mathbf{P}(S_N \geq b) = \mathbf{P}(S'_{N'} \geq b)$ ;
- page 4, after (6): recall that  $c_i \geq b$ ;
- page 4, Section 2: remove the first sentence;
- page 4, line -10: I would give more details and explanations on the connection between  $\mathbf{ET}$  and the change point problem;
- page 5, line -6: replace the word 'sequences' by 'random variables'