

SIMPLE GROUPS WITH NARROW PRIME SPECTRUM:
EXTENDED LISTA. V. ZAVARNITSINE *Communicated by I.B. GORSHKOV*

Abstract: Generalising a previous result, we determine all non-abelian finite simple groups whose order has largest prime divisor not exceeding 10^4 . The computer code for this and similar calculations is made available.

Keywords: simple group, order, prime factor, n -primary group

Introduction

This paper continues the work of [4] which has proved useful. In [4], all non-abelian finite simple groups with order having largest prime divisor not exceeding 1000 were determined. Here we extend this bound to 10000, thereby proving the following.

Theorem 1. *There are 15072 isomorphism types of finite non-abelian simple groups whose order has all prime divisors less than 10000.*

Recall from [4] that, for a finite group G , its *prime spectrum*, denoted by $\pi(G)$, is the set of prime divisors of $|G|$. Given a prime p , we write \mathfrak{S}_p for

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the set of non-abelian finite simple groups G satisfying

$$p \in \pi(G) \subseteq \{2, 3, 5, \dots, p\}.$$

The sets \mathfrak{S}_p , $p \geq 5$, are finite and always contain the *generic* groups

$$L_2(p), A_p, A_{p+1}, \dots, A_{p'-1},$$

where p' is the smallest prime exceeding p . In particular, there are $p' - p + 1$ such groups in \mathfrak{S}_p . The primes p for which \mathfrak{S}_p consists solely of generic groups are called *generic primes*. The non-generic elements of \mathfrak{S}_p , when they exist, are of particular interest.

The 13100 groups obtained in the present paper (which, together with the 1972 already listed in [4], give a total of 15072 groups) can be inferred from Tables 1 and 2. In Table 1, we list the 301 generic primes between 1000 and 10000. In Table 2, we list the 3041 non-generic groups G from the union

$$\mathfrak{S}_{1009} \cup \dots \cup \mathfrak{S}_{9973}$$

of the sets \mathfrak{S}_p corresponding to the 760 remaining non-generic primes between 1000 and 10000.

The notation for simple groups in Table 2 follows that of [1], except the sizes of defining fields bigger than 100 are written exponentially, e. g., $L_2(3^7)$ in place of $L_2(2187)$.

As is apparent from the tables, the overwhelming majority of groups are generic. It is reasonable to expect alternating groups to dominate the set \mathfrak{S}_p asymptotically.

Curiously, the largest number 44 of non-generic groups in \mathfrak{S}_p for $p < 1000$ is attained at $p = 257$ (a Fermat prime) and remains so for all $p < 10000$. We have no example of \mathfrak{S}_p with more than 44 non-generic elements. The second largest value, 39, occurs at $p = 6481$ which is the greatest prime factor of $3^{12} + 1$.

The calculations of this paper (and, retrospectively, those of [4]) can be verified using the GAP [2] code provided in [5]. Specifically, we implement a universal function

$$\text{SimpleGroupsPi}(\text{pi}) \tag{1}$$

which accepts an arbitrary set of primes pi and returns (codes of) all non-abelian finite simple groups G satisfying $\pi(G) \subseteq \text{pi}$.

The idea behind the implemented algorithm is due to V. D. Mazurov and is outlined in [3, p. 51]. Roughly, any simple group G with $\pi(G) \subseteq \pi$ satisfies $G \in \mathcal{S} \cup \mathcal{A}_\pi \cup \mathcal{L}_\pi$, where \mathcal{S} is the set of 26 sporadic groups, \mathcal{A}_π is the set of alternating groups A_n with $n \leq p_0 - 1$, where p_0 is the smallest prime greater than all primes in π , and \mathcal{L}_π is the set of groups of Lie type defined over a field of order p^k with $p \in \pi$ and having rank l_p , where

$$k \leq t_p = \max_{r \in \pi \setminus \{p\}} \text{ord}_r p,$$

and $l_p \leq \max\{8, t_p\}$. Hence, finding all such groups G reduces to checking the orders of finitely many groups.

The running time of function (1) depends on both the cardinality of \mathbf{pi} and the size of its largest element: the computations with all primes up to 1000 take approximately 1 minute, while those with primes less than 10000 require 25 hours. It is therefore impractical to apply this linear implementation directly to, say, all primes up to 10^5 . However, the algorithm is highly parallelisable.

On the other hand, the program runs quickly when \mathbf{pi} is small, even if it contains large primes. Thus, in [5, Example 1], we find all 13 simple groups

$$A_5, A_6, U_5(2), L_2(3^5), S_4(3), L_2(11), L_2(11^2), \\ S_4(11), U_3(11), U_4(11), U_5(11), M_{11}, M_{12}$$

with prime spectrum a subset of

$$\pi(U_5(11)) = \{2, 3, 5, 11, 37, 61, 13421\}$$

within seconds, where $U_5(11)$ is notable for having the largest prime divisor of its order, 13421, among all groups listed in the Atlas table [1, p. 239]. Calculations of this sort with a custom set \mathbf{pi} might be useful for applications.

Theorem 1 results from running (1) with

$$\mathbf{pi} = \{2, 3, \dots, 9973\}.$$

Tables 1 and 2 are obtained after sorting the output according to the maximal prime factor and determining whether \mathfrak{S}_p is generic, see [5, Example 3] for details.

Another natural stratification of the groups from Theorem 1 is by the size of their prime spectrum. Excluding the alternating groups, the largest size of prime spectrum turns out to be 24 attained for the four groups

$$L_{15}(4), S_{30}(2), O_{32}^+(2), U_{15}(4), \quad (2)$$

of which the first three have the same prime spectrum equal to

$$\{2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 41, 43, 73, 89, \\ 113, 127, 151, 241, 257, 331, 683, 2731, 8191\}. \quad (3)$$

The second largest size, 23, is attained for just two non-alternating groups, $O_{30}^+(2)$ and $O_{30}^-(2)$, whose prime spectrum can be obtained from (3) by removing 331 and 151, respectively.

More generally, for every $n = 3, \dots, 24$, we list in [5, Example 4] explicitly the sets $\mathfrak{K}_n = \mathfrak{K}_{n,1229}$ of all n -primary groups (also known as K_n -groups) from Theorem 1. Here $\mathfrak{K}_{n,m}$ denotes the set of non-abelian simple groups whose orders have exactly n distinct prime factors all of which do not exceed the m -th prime p_m . We have $\mathfrak{K}_{n,m_1} \subseteq \mathfrak{K}_{n,m_2}$ whenever $m_1 \leq m_2$. Note that 1229 is the index of 9973, the largest prime less than 10000.

The sizes of \mathfrak{K}_n for $n \leq 24$ are as follows:

n	3	4	5	6	7	8	9	
$ \mathfrak{K}_n $	8	65	349	715	595	628	828	
n	10	11	12	13	14	15	16	
$ \mathfrak{K}_n $	641	398	309	238	119	87	62	
n	17	18	19	20	21	22	23	24
$ \mathfrak{K}_n $	32	12	18	7	16	15	8	12

Clearly, \mathfrak{K}_n contains the $p_{n+1} - p_n$ alternating groups

$$A_{p_n}, A_{p_n+1}, \dots, A_{p_{n+1}-1}$$

for every $n = 3, \dots, 1229$ and, in fact, only those groups for $n > 24$. For example, \mathfrak{K}_{24} consists of A_{89}, \dots, A_{96} plus the four groups in (2), a total of 12 groups.

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The tables

Table 1: Primes $p \in \{1000, \dots, 10000\}$ with generic \mathfrak{S}_p

1009, 1013, 1019, 1033, 1039, 1097, 1103, 1151, 1163, 1187, 1193,
1213, 1217, 1249, 1259, 1279, 1307, 1319, 1361, 1381, 1409, 1439,
1453, 1481, 1523, 1559, 1579, 1627, 1667, 1669, 1721, 1733, 1777,
1811, 1847, 1879, 1901, 1907, 1933, 1949, 1997, 2003, 2011, 2029,
2063, 2069, 2087, 2129, 2137, 2179, 2221, 2239, 2341, 2351, 2357,
2377, 2381, 2399, 2423, 2447, 2459, 2477, 2543, 2549, 2593, 2647,
2659, 2663, 2699, 2711, 2741, 2857, 2879, 2887, 2909, 2927, 2963,
3023, 3061, 3067, 3119, 3163, 3167, 3191, 3209, 3217, 3271, 3299,
3329, 3371, 3407, 3469, 3491, 3539, 3677, 3697, 3719, 3733, 3761,
3767, 3797, 3803, 3821, 3823, 3847, 3877, 3911, 3923, 3929, 3943,
3989, 4001, 4019, 4127, 4139, 4153, 4157, 4159, 4231, 4241, 4259,
4339, 4349, 4397, 4409, 4447, 4451, 4463, 4507, 4517, 4547, 4583,
4663, 4703, 4759, 4871, 4919, 4931, 4943, 4993, 4999, 5003, 5011,
5021, 5039, 5081, 5147, 5179, 5273, 5279, 5297, 5303, 5309, 5333,
5387, 5393, 5399, 5407, 5417, 5449, 5471, 5501, 5519, 5521, 5563,
5651, 5669, 5689, 5737, 5741, 5783, 5839, 5897, 5903, 5939, 5953,
5981, 5987, 6011, 6047, 6101, 6113, 6131, 6199, 6203, 6221, 6271,
6329, 6361, 6563, 6599, 6653, 6689, 6709, 6719, 6761, 6791, 6857,
6869, 6883, 6947, 7001, 7013, 7019, 7043, 7069, 7109, 7211, 7229,
7243, 7247, 7331, 7349, 7393, 7411, 7417, 7451, 7457, 7487, 7517,
7523, 7541, 7547, 7573, 7589, 7591, 7643, 7691, 7741, 7757, 7793,
7817, 7823, 7829, 7901, 7937, 7951, 8017, 8053, 8059, 8081, 8087,
8123, 8167, 8171, 8231, 8233, 8293, 8311, 8353, 8419, 8431, 8467,
8513, 8543, 8627, 8677, 8693, 8699, 8741, 8753, 8803, 8819, 8849,
8963, 8969, 9013, 9029, 9041, 9059, 9137, 9151, 9203, 9293, 9311,
9319, 9323, 9371, 9397, 9413, 9437, 9473, 9497, 9521, 9533, 9539,
9547, 9613, 9623, 9629, 9719, 9743, 9749, 9767, 9769, 9781, 9787,
9803, 9829, 9857, 9973

Table 2: Non-generic simple groups G with $p \in \pi(G) \subseteq \{2, 3, 5, \dots, p\}$ for $1000 < p < 10000$

p	$ \mathfrak{S}_p $	G
1021	16	$L_2(647^2), S_4(647), L_2(653^3), G_2(653), U_3(653)$
1031	4	$U_3(1031)$
1049	4	$L_3(1049)$
1051	15	$L_2(181^3), G_2(181), U_3(181), U_3(1051)$
1061	6	$L_2(103^2), S_4(103), U_4(103)$
1063	12	$L_3(7^3), L_4(7^3), L_3(719), L_2(719^3), G_2(719)$
1069	21	$U_3(983), L_3(1069)$
1087	28	$L_3(257), L_2(257^3), G_2(257), L_3(829), L_4(829), L_3(829^2), L_2(829^3), S_6(829), O_7(829), O_8^+(829), G_2(829), L_3(1087), L_4(1087), L_2(1087^2), L_3(1087^2), L_2(1087^3), S_4(1087), S_6(1087), O_7(1087), O_8^+(1087), G_2(1087), U_3(1087), U_4(1087)$
1091	4	$U_3(1091)$
1093	34	$L_7(3), L_8(3), L_9(3), L_{10}(3), L_7(9), L_2(3^7), L_8(9), L_9(9), S_{14}(3), S_{16}(3), S_{18}(3), O_{15}(3), O_{17}(3), O_{19}(3), O_{14}^+(3), O_{16}^+(3), O_{18}^+(3), O_{20}^+(3), O_{16}^-(3), O_{18}^-(3), E_7(3), L_3(151), L_4(151), L_2(563^2), S_4(563), U_4(563), L_3(941), L_2(941^3), G_2(941)$
1109	21	$L_3(1109), L_4(1109), L_2(1109^2), L_3(1109^2), L_2(1109^3), S_4(1109), S_6(1109), O_7(1109), O_8^+(1109), G_2(1109), U_3(1109), U_4(1109)$
1117	16	$L_2(11^6), S_4(11^3), G_2(11^2), {}^3D_4(11), U_3(11^2), U_3(23^3), L_2(997^3), G_2(997), U_3(997)$
1123	9	$L_2(1123^2), S_4(1123)$
1129	33	$L_4(31^2), L_2(31^4), S_8(31), S_4(31^2), O_9(31), O_8^-(31), L_3(1129), L_2(1129^3), G_2(1129), U_3(1129)$
1153	15	$U_3(503), L_2(1013^2), S_4(1013), L_3(1153)$
1171	14	$U_3(421), U_4(421), U_3(751)$

p	$ \mathfrak{S}_p $	G
1181	22	$L_{10}(9), L_5(3^4), L_2(3^{10}), S_{20}(3), S_{10}(9), S_4(3^5), O_{21}(3), O_{11}(9), O_{12}^+(9), O_{10}^-(9), O_{20}^-(3), O_{22}^-(3), U_5(9), U_6(9), U_4(3^5)$
1201	37	$L_4(49), L_2(7^4), L_3(7^4), L_2(7^{12}), S_8(7), S_4(49), S_6(49), S_4(7^6), O_9(7), O_7(49), O_8^+(49), O_8^-(7), O_{10}^-(7), G_2(7^4), F_4(7), U_8(7), U_4(49), U_3(7^4), L_2(571^3), G_2(571), U_3(571), L_2(631^3), G_2(631), U_3(631)$
1223	9	$L_2(1223^2), S_4(1223)$
1229	7	$L_2(1229^2), S_4(1229), U_3(1229), U_4(1229)$
1231	9	$U_3(127), L_3(1231)$
1237	17	$L_2(691^2), S_4(691), U_3(937), L_3(1237)$
1277	8	$L_4(113), L_2(113^2), S_4(113), L_2(1277^2), S_4(1277)$
1283	8	$L_3(1283)$
1289	5	$L_2(479^2), S_4(479)$
1291	9	$U_3(347), L_3(1291)$
1297	9	$L_2(1297^2), S_4(1297), U_3(1297), U_4(1297)$
1301	5	$L_2(1301^2), S_4(1301)$
1303	7	$L_2(1303^2), S_4(1303)$
1321	28	$L_5(2^{12}), L_2(2^{30}), S_{10}(64), S_4(2^{15}), O_{12}^+(64), O_{10}^-(64), G_2(2^{10}), {}^3D_4(32), U_5(64), U_3(2^{10}), U_6(64), L_4(257), L_2(257^2), L_3(257^2), S_4(257), S_6(257), O_7(257), O_8^+(257), U_4(257), Sz(2^{15}), {}^2F_4(32)$
1327	42	$L_3(347), L_2(347^3), G_2(347), L_2(1327^2), S_4(1327), U_3(1327), U_4(1327)$
1367	8	$L_3(1367)$
1373	11	$L_2(1373^2), S_4(1373)$
1399	13	$U_3(1009), U_3(1399)$
1423	6	$L_3(643)$
1427	5	$L_2(1427^2), S_4(1427)$
1429	9	$L_4(809), L_2(809^2), S_4(809), L_3(1429)$

continued

continued

p	$ \mathfrak{S}_p $	G
1433	11	$L_2(1433^2), S_4(1433), U_3(1433), U_4(1433)$
1447	7	$U_3(743), U_4(743)$
1451	4	$L_3(1451)$
1459	14	$L_3(1459)$
1471	14	$L_3(251), L_4(251), L_3(1471)$
1483	7	$L_2(1483^2), S_4(1483)$
1487	7	$L_2(1487^2), S_4(1487), U_3(1487), U_4(1487)$
1489	6	$U_3(1489)$
1493	13	$L_2(1061^2), S_4(1061), L_3(1493), L_4(1493), L_2(1493^2), S_4(1493)$
1499	14	$U_3(1499)$
1511	14	$L_3(1511)$
1531	15	$U_3(647), U_4(647)$
1543	8	$L_3(1543)$
1549	7	$L_2(1549^2), S_4(1549)$
1553	9	$L_2(1553^2), S_4(1553)$
1567	10	$L_3(1031), L_2(1031^3), G_2(1031), L_2(1567^2), S_4(1567)$
1571	10	$L_3(1571)$
1583	16	$U_3(1583)$
1597	10	$U_3(223), L_3(1597), L_4(1597), L_2(1597^2), S_4(1597)$
1601	11	$L_3(1601), L_2(1601^3), G_2(1601), U_3(1601)$
1607	5	$L_2(1607^2), S_4(1607)$
1609	16	$L_3(251^2), L_2(251^3), S_6(251), O_7(251), O_8^+(251), G_2(251), U_3(251), U_4(251), L_2(523^2), S_4(523), U_4(523)$
1613	10	$L_2(127^2), S_4(127), U_4(127)$
1619	4	$U_3(1619)$
1621	8	$U_3(89^2)$
1637	27	$L_2(1321^2), S_4(1321), L_3(1637), L_4(1637), L_2(1637^2), S_4(1637)$
1657	12	$U_3(71), L_2(239^4), S_4(239^2), L_2(1657^2), S_4(1657)$
1663	6	$L_3(1663)$

continued

p	$ \mathfrak{S}_p $	G
1693	16	$L_3(433), L_3(1259), L_4(1601), L_2(1601^2), L_3(1601^2), S_4(1601), S_6(1601), O_7(1601), O_8^+(1601), U_4(1601), L_3(1693)$
1697	6	$L_4(1283), L_2(1283^2), S_4(1283)$
1699	20	$L_3(397), L_2(397^3), G_2(397), L_3(1301), L_4(1301), L_2(1699^2), S_4(1699), U_3(1699), U_4(1699)$
1709	15	$L_2(1319^2), S_4(1319)$
1723	21	$L_3(41), L_4(41), L_3(41^2), L_2(41^3), S_6(41), O_7(41), O_8^+(41), G_2(41), L_2(1723^2), S_4(1723)$
1741	14	$L_5(5^3), L_3(5^5), L_2(59^2), L_2(59^4), S_4(59), S_4(59^2), U_4(59)$
1747	9	$L_2(1747^2), S_4(1747)$
1753	11	$L_2(1571^3), G_2(1571), U_3(1571), U_3(1753)$
1759	21	$U_3(509), U_4(509)$
1783	19	$L_3(193), L_4(193), L_3(1783), L_4(1783), L_2(1783^2), L_3(1783^2), L_2(1783^3), S_4(1783), S_6(1783), O_7(1783), O_8^+(1783), G_2(1783), U_3(1783), U_4(1783)$
1787	5	$L_2(1787^2), S_4(1787)$
1789	25	$L_3(1637^2), L_2(1637^3), S_6(1637), O_7(1637), O_8^+(1637), G_2(1637), U_3(1637), U_4(1637), L_3(1789), L_4(1789), L_2(1789^2), S_4(1789)$
1801	23	$L_5(32), L_6(32), L_3(73), L_4(73), L_3(73^2), L_2(73^3), S_6(73), O_7(73), O_8^+(73), G_2(73), L_2(977^2), S_4(977)$
1823	21	$L_3(1823), L_4(1823), L_2(1823^2), L_3(1823^2), L_2(1823^3), S_4(1823), S_6(1823), O_7(1823), O_8^+(1823), G_2(1823), U_3(1823), U_4(1823)$
1831	19	$U_3(673), L_3(1831)$
1861	17	$L_4(61), L_2(61^2), L_3(61^2), S_4(61), S_6(61), O_7(61), O_8^+(61), U_4(61), L_2(1861^2), S_4(1861)$
1867	6	$U_3(1033)$
1871	4	$U_3(1871)$
1873	7	$U_3(1759), L_3(1873)$

continued

p	$ \mathfrak{S}_p $	G
1877	8	$L_4(137), L_2(137^2), S_4(137), L_2(1877^2), S_4(1877)$
1889	17	$L_2(331^2), S_4(331), L_2(1889^2), S_4(1889)$
1913	25	$L_2(1201^2), S_4(1201), L_3(1913), L_4(1913), L_2(1913^2), S_4(1913)$
1931	7	$L_2(1931^2), S_4(1931), U_3(1931), U_4(1931)$
1951	24	$U_3(1951)$
1973	8	$U_3(1973)$
1979	10	$U_3(1979)$
1987	16	$L_3(647), L_4(647), L_3(647^2), L_2(647^3), S_6(647), O_7(647), O_8^+(647), G_2(647), L_3(1987)$
1993	18	$L_2(41^6), S_4(41^3), G_2(41^2), {}^3D_4(41), U_3(41^2), L_3(313^2), L_2(313^3), S_6(313), O_7(313), O_8^+(313), G_2(313), U_3(313), U_4(313)$
1999	13	$L_3(809^2), L_2(809^3), S_6(809), O_7(809), O_8^+(809), G_2(809), U_3(809), U_4(809)$
2017	16	$L_4(229), L_2(229^2), S_4(229), U_3(1723), U_4(1723)$
2027	4	$L_3(2027)$
2039	16	$L_3(2039)$
2053	15	$L_3(197), L_2(197^3), G_2(197), L_3(2053)$
2081	6	$L_2(1979^2), S_4(1979), U_4(1979)$
2083	7	$L_3(449), U_3(2083)$
2089	12	$U_3(827)$
2099	17	$L_2(2099^2), S_4(2099), U_3(2099), U_4(2099)$
2111	5	$L_2(2111^2), S_4(2111)$
2113	34	$L_2(2^{22}), S_4(2^{11}), U_{11}(4), U_{12}(4), U_{13}(4), U_{14}(4), U_{15}(4), L_3(439^2), L_2(439^3), S_6(439), O_7(439), O_8^+(439), G_2(439), U_3(439), U_4(439), L_3(2113), Sz(2^{11})$
2131	10	$L_2(1663^3), G_2(1663), U_3(1663)$
2141	6	$L_2(419^2), S_4(419), U_4(419)$
2143	14	$L_3(349), L_2(2143^2), S_4(2143)$

continued

p	$ \mathfrak{S}_p $	G
2153	11	$L_2(2153^2), S_4(2153)$
2161	29	$L_3(593), L_4(593), L_3(593^2), L_2(593^3), S_6(593), O_7(593), O_8^+(593), G_2(593), L_3(1567), L_4(1567)$
2203	6	$U_3(2203)$
2207	9	$L_2(2207^2), S_4(2207)$
2213	10	$U_3(2213)$
2237	5	$L_2(1021^2), S_4(1021)$
2243	10	$L_3(2243)$
2251	24	$L_2(19^5), U_5(19), U_6(19), U_3(709), L_2(1543^3), G_2(1543), U_3(1543)$
2267	7	$L_3(2267), L_2(2267^3), G_2(2267), U_3(2267)$
2269	16	$U_7(27), U_3(3^7), L_3(83^2), L_2(83^3), S_6(83), O_7(83), O_8^+(83), G_2(83), U_3(83), U_4(83), {}^2G_2(3^7)$
2273	10	$U_3(2273)$
2281	15	$L_4(1571), L_2(1571^2), L_3(1571^2), S_4(1571), S_6(1571), O_7(1571), O_8^+(1571), U_4(1571)$
2287	9	$U_3(1483), U_4(1483)$
2293	12	$U_3(113^2), L_3(1303), L_4(1303), L_4(1693), L_2(1693^2), S_4(1693), L_3(2293)$
2297	15	$L_2(2297^2), S_4(2297)$
2309	7	$L_2(1621^2), S_4(1621), L_2(2309^2), S_4(2309)$
2311	28	$U_3(883), L_2(1429^3), G_2(1429), U_3(1429), L_3(2311)$
2333	9	$L_2(2333^2), S_4(2333)$
2339	4	$U_3(2339)$
2347	7	$U_3(1063), L_3(2347)$
2371	8	$U_3(1907)$
2383	10	$L_3(1103), L_3(1279), U_3(2383)$
2389	13	$L_3(1699), L_4(1699), L_3(1699^2), L_2(1699^3), S_6(1699), O_7(1699), O_8^+(1699), G_2(1699)$
2393	14	$L_4(971), L_2(971^2), S_4(971), L_3(2393), L_2(2393^3), G_2(2393), U_3(2393)$

continued

p	$ \mathfrak{S}_p $	G	p	$ \mathfrak{S}_p $	G
2411	10	$U_5(13), U_6(13), U_3(2411)$	2729	6	$L_2(1627^2), S_4(1627), U_3(2729)$
2417	9	$L_2(2417^2), S_4(2417)$	2731	16	$O_{26}^-(2), U_{13}(2), U_{14}(2), U_{15}(2), U_{16}(2)$
2437	9	$L_4(2039), L_2(2039^2), S_4(2039), L_3(2351)$	2749	7	$L_3(2153), L_4(2153)$
2441	9	$L_2(2441^2), S_4(2441)$	2753	17	$L_2(2753^2), S_4(2753)$
2467	8	$U_3(2251)$	2767	13	$L_2(2767^2), S_4(2767)$
2473	6	$L_3(2473)$	2777	15	$L_2(2777^2), S_4(2777)$
2503	25	$U_3(1277), U_4(1277), L_3(2503), L_4(2503), L_2(2503^2), S_4(2503)$	2789	6	$L_2(167^2), S_4(167), U_3(2789)$
2521	15	$L_2(71^2), S_4(71), U_4(71), U_3(97^2)$	2791	8	$L_3(2699)$
2531	11	$L_2(2531^2), S_4(2531)$	2797	6	$U_3(1697)$
2539	13	$L_3(307^2), L_2(307^3), S_6(307), O_7(307), O_8^+(307), G_2(307), U_3(307), U_4(307)$	2801	27	$L_5(7), L_6(7), L_5(49), L_2(7^5), L_6(49), S_{10}(7), S_{12}(7), O_{11}(7), O_{13}(7), O_{10}^+(7), O_{12}^+(7), O_{12}^-(7), O_{14}^-(7), E_6(7), L_4(1543), L_2(1543^2), L_3(1543^2), S_4(1543), S_6(1543), O_7(1543), O_8^+(1543), U_4(1543), L_2(2801^2), S_4(2801)$
2551	11	$L_3(2551), L_4(2551), L_2(2551^2), S_4(2551)$	2803	18	$L_3(2389)$
2557	25	$L_3(1721), L_3(2557)$	2819	16	$L_3(2819)$
2579	17	$L_2(2579^2), S_4(2579), U_3(2579), U_4(2579)$	2833	14	$L_3(1301^2), L_2(1301^3), S_6(1301), O_7(1301), O_8^+(1301), G_2(1301), U_3(1301), U_4(1301), U_3(2833)$
2591	4	$L_3(2591)$	2837	8	$L_3(2837)$
2609	15	$L_2(389^2), S_4(389), L_3(2609), L_2(2609^3), G_2(2609), U_3(2609)$	2843	13	$L_2(2843^2), S_4(2843), U_3(2843), U_4(2843)$
2617	8	$U_3(1553), U_4(1553), U_3(2617)$	2851	9	$U_5(107), U_6(107)$
2621	15	$L_2(2621^2), S_4(2621)$	2861	22	$L_5(149), L_2(2861^2), S_4(2861)$
2633	19	$L_2(1409^2), S_4(1409), L_2(2633^2), S_4(2633)$	2897	9	$L_2(1777^2), S_4(1777)$
2657	7	$L_4(163), L_2(163^2), L_5(163), S_4(163)$	2903	9	$L_2(2903^2), S_4(2903)$
2671	8	$L_3(2671)$	2917	13	$L_2(2917^2), S_4(2917)$
2677	10	$L_3(1033), L_2(1033^3), G_2(1033)$	2939	19	$L_3(2939), L_4(2939), L_2(2939^2), S_4(2939)$
2683	6	$L_3(2683)$	2953	14	$L_3(2153^2), L_2(2153^3), S_6(2153), O_7(2153), O_8^+(2153), G_2(2153), U_3(2153), U_4(2153), U_3(2953)$
2687	4	$U_3(2687)$	2957	8	$U_3(2957)$
2689	7	$L_3(2297), L_4(2297)$	2969	6	$U_7(23), L_2(2969^2), S_4(2969)$
2693	10	$L_2(859^2), S_4(859), U_4(859)$	2971	43	$U_3(2971), U_4(2971), L_3(2971), L_4(2971), L_2(2971^2), L_3(2971^2), L_2(2971^3), S_4(2971), S_6(2971), O_7(2971), O_8^+(2971), G_2(2971), U_3(2971), U_4(2971)$
2707	15	$L_3(1327), L_4(1327), L_3(1327^2), L_2(1327^3), S_6(1327), O_7(1327), O_8^+(1327), G_2(1327), L_2(2707^2), S_4(2707)$			
2713	9	$L_2(887^2), S_4(887)$			
2719	12	$L_3(1453)$			

continued

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p	$ \mathfrak{S}_p $	G	p	$ \mathfrak{S}_p $	G
2999	4	$L_3(2999)$	3319	9	$L_3(3319), L_4(3319), L_2(3319^2), S_4(3319)$
3001	15	$L_3(3001), L_2(3001^3), G_2(3001), U_3(3001)$	3323	11	$L_2(3323^2), S_4(3323), U_3(3323), U_4(3323)$
3011	11	$L_2(3011^2), S_4(3011)$	3331	14	$L_3(1867)$
3019	18	$L_3(239), L_4(239), L_3(239^2), L_2(239^3), L_4(239^2), S_6(239), S_8(239), O_7(239), O_9(239), O_8^+(239), O_8^-(239), G_2(239), L_3(3019)$	3343	7	$L_2(3343^2), S_4(3343)$
3037	8	$L_4(281), L_2(281^2), S_4(281)$	3347	14	$L_3(3347)$
3041	17	$L_4(2267), L_2(2267^2), L_3(2267^2), S_4(2267), S_6(2267), O_7(2267), O_8^+(2267), U_4(2267)$	3359	7	$L_3(3359), L_4(3359), L_2(3359^2), S_4(3359)$
3049	15	$L_2(137^4), S_4(137^2)$	3361	14	$U_3(421^2), L_2(3361^2), S_4(3361)$
3079	9	$L_3(43^3), L_2(547^3), G_2(547), U_3(547)$	3373	22	$U_3(2719), L_3(3373), L_4(3373), L_2(3373^2), S_4(3373)$
3083	11	$L_2(3083^2), S_4(3083), U_3(3083), U_4(3083)$	3389	7	$L_3(3389), L_4(3389), L_2(3389^2), S_4(3389)$
3089	22	$L_3(3089)$	3391	18	$U_3(3391)$
3109	13	$L_2(727^2), S_4(727)$	3413	24	$L_4(1471), L_2(1471^2), S_4(1471)$
3121	23	$L_4(79), L_2(79^2), L_2(79^4), S_4(79), S_4(79^2), L_3(1999)$	3433	25	$L_3(269^2), L_2(269^3), S_6(269), O_7(269), O_8^+(269), G_2(269), U_3(269), U_4(269)$
3137	31	$L_2(3137^2), S_4(3137), U_3(3137), U_4(3137)$	3449	10	$U_3(3449)$
3169	25	$L_3(97), L_4(97), L_3(97^2), L_2(97^3), L_2(97^6), S_6(97), S_4(97^3), O_7(97), O_8^+(97), G_2(97), G_2(97^2), {}^3D_4(97)$	3457	7	$L_2(2749^2), S_4(2749)$
3181	8	$U_3(2741)$	3461	7	$L_4(1453), L_2(1453^2), S_4(1453), L_3(3461)$
3187	8	$L_3(1871), L_2(1871^3), G_2(1871)$	3463	10	$L_3(367), L_2(367^3), G_2(367), L_2(3463^2), S_4(3463)$
3203	11	$L_3(3203), L_4(3203), L_2(3203^2), S_4(3203)$	3467	4	$U_3(3467)$
3221	11	$L_5(11), L_6(11)$	3499	17	$U_3(157), U_4(157), U_3(3343), U_4(3343)$
3229	26	$L_2(839^2), S_4(839), L_3(3229)$	3511	11	$U_3(757), U_4(757), L_2(3511^2), S_4(3511)$
3251	5	$L_2(3251^2), S_4(3251)$	3517	12	$U_3(3259)$
3253	8	$L_3(1439), L_2(3253^2), S_4(3253)$	3527	7	$L_3(3527), L_2(3527^3), G_2(3527), U_3(3527)$
3257	4	$L_3(3257)$	3529	9	$L_2(449^3), G_2(449), U_3(449), U_3(3529)$
3259	15	$U_3(853), U_4(853)$	3533	8	$U_3(3533)$
3301	10	$L_2(2089^2), S_4(2089), U_3(3011^2)$	3541	29	$L_3(59), L_4(59), L_5(59), L_6(59), L_3(59^2), L_2(59^3), L_4(59^2), S_6(59), S_8(59), O_7(59), O_9(59), O_8^+(59), O_{10}^+(59), O_8^-(59), G_2(59), U_3(59^3), L_2(2689^2), S_4(2689), L_3(3541), L_4(3541), L_2(3541^2), S_4(3541)$
3307	9	$L_2(3307^2), S_4(3307)$			
3313	9	$L_3(1123), L_4(1123)$			

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p	$ \mathfrak{S}_p $	G	p	$ \mathfrak{S}_p $	G
3547	14	$U_3(1163), L_2(3547^2), S_4(3547)$	3793	12	$L_2(1069^3), G_2(1069), U_3(1069),$ $L_3(3793), L_4(3793), L_2(3793^2),$ $S_4(3793)$
3557	5	$L_2(3557^2), S_4(3557)$	3833	37	$L_4(19^2), L_2(19^4), L_5(19^2),$ $L_6(19^2), L_3(19^4), S_8(19),$ $S_4(19^2), S_{10}(19), S_{12}(19),$ $S_6(19^2), O_9(19), O_{11}(19),$ $O_{13}(19), O_7(19^2), O_{10}^+(19),$ $O_{12}^+(19), O_8^+(19^2), O_8^-(19),$ $O_{10}^-(19), O_{12}^-(19), F_4(19),$ $U_4(19^2)$
3559	14	$U_3(3559)$	3851	13	$L_{11}(3), L_{12}(3), L_{11}(9), L_2(3^{11}),$ $S_{22}(3), O_{23}(3), O_{22}^+(3), O_{24}^+(3),$ $U_5(53), U_6(53)$
3571	23	$L_3(103), L_4(103), L_3(103^2),$ $L_2(103^3), S_6(103), O_7(103),$ $O_8^+(103), G_2(103), L_3(3467),$ $L_2(3467^3), G_2(3467), L_3(3571)$	3853	13	$L_3(2713), U_3(3853)$
3581	6	$L_2(3217^2), S_4(3217), L_3(3581)$	3863	17	$L_2(3863^2), S_4(3863)$
3583	14	$U_3(1039), L_2(3583^2), S_4(3583)$	3881	19	$L_4(197), L_2(197^2), L_5(197),$ $L_6(197), L_3(197^2), S_4(197),$ $S_6(197), O_7(197), O_8^+(197),$ $U_4(197)$
3593	18	$L_4(1153), L_2(1153^2), S_4(1153)$	3889	22	$L_2(1999^3), G_2(1999), U_3(1999)$
3607	13	$L_3(1399), L_2(1399^3), G_2(1399),$ $L_3(2207), L_4(2207), L_3(3607)$	3907	7	$L_2(3907^2), S_4(3907)$
3613	6	$U_3(3613)$	3917	7	$L_3(3917), L_2(3917^3), G_2(3917),$ $U_3(3917)$
3617	12	$L_2(2383^2), S_4(2383), U_4(2383),$ $L_2(3617^2), S_4(3617)$	3919	7	$L_3(2749), L_4(2749)$
3623	13	$L_3(3623), L_2(3623^3), G_2(3623),$ $U_3(3623)$	3931	15	$L_3(617), L_3(3313)$
3631	12	$U_5(523), L_3(3631), L_2(3631^3),$ $G_2(3631), U_3(3631)$	3947	25	$L_2(3947^2), S_4(3947), U_3(3947),$ $U_4(3947)$
3637	8	$U_3(3637)$	3967	25	$U_3(3079), U_3(3967)$
3643	20	$U_3(3221), L_2(3643^2), S_4(3643)$	4003	9	$L_2(823^3), G_2(823), U_3(823),$ $U_3(3181)$
3659	15	$L_2(3659^2), S_4(3659)$	4007	11	$L_2(4007^2), S_4(4007), U_3(4007),$ $U_4(4007)$
3671	5	$L_2(3671^2), S_4(3671)$	4013	8	$U_3(4013)$
3673	8	$L_3(1151), L_3(2521), L_3(3673)$	4021	16	$L_2(7^{10}), S_4(7^5), U_5(49), U_6(49),$ $L_2(47^6), S_4(47^3), G_2(47^2),$ ${}^3D_4(47), U_3(47^2)$
3691	9	$U_3(3217), U_4(3217)$	4027	43	$L_3(2207^2), L_2(2207^3), S_6(2207),$ $O_7(2207), O_8^+(2207), G_2(2207),$ $U_3(2207), U_4(2207), L_3(4027),$ $L_4(4027), L_2(4027^2), L_3(4027^2),$ $L_2(4027^3), S_4(4027), S_6(4027),$ $O_7(4027), O_8^+(4027), G_2(4027),$ $U_3(4027), U_4(4027)$
3701	13	$L_4(1279), L_2(1279^2), S_4(1279),$ $L_3(3701)$	3779	16	$L_3(3779)$
3709	22	$L_3(499^2), L_2(499^3), S_6(499),$ $O_7(499), O_8^+(499), G_2(499),$ $U_3(499), U_4(499), L_2(1609^2),$ $S_4(1609), U_3(3709)$			
3727	10	$U_3(2539), L_2(3727^2), S_4(3727)$			
3739	24	$L_3(3739)$			
3769	31	$L_3(463), L_4(463), L_3(463^2),$ $L_2(463^3), S_6(463), O_7(463),$ $O_8^+(463), G_2(463), L_3(3769),$ $L_4(3769), L_2(3769^2), L_3(3769^2),$ $L_2(3769^3), S_4(3769), S_6(3769),$ $O_7(3769), O_8^+(3769), G_2(3769),$ $U_3(3769), U_4(3769)$			

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p	$ \mathfrak{S}_p $	G
4049	4	$U_3(4049)$
4051	13	$L_2(2^{25}), U_5(32), U_6(32),$ $L_3(797), L_3(3253), L_4(3253)$
4057	19	$U_3(1409), U_4(1409)$
4073	11	$L_3(4073), L_2(4073^3), G_2(4073),$ $U_3(4073)$
4079	14	$U_3(4079)$
4091	4	$U_3(4091)$
4093	8	$U_3(3191)$
4099	15	$L_3(2017), L_3(2081)$
4111	20	$U_5(41), U_6(41), L_3(4111)$
4129	14	$L_3(1979), L_4(1979), L_3(1979^2),$ $L_2(1979^3), S_6(1979), O_7(1979),$ $O_8^+(1979), G_2(1979), U_3(4129)$
4133	10	$L_2(733^2), S_4(733), L_3(4133)$
4177	31	$L_2(457^2), S_4(457), L_2(1103^3),$ $G_2(1103), U_3(1103), U_3(4177)$
4201	12	$U_3(1013^2)$
4211	8	$U_3(4211)$
4217	7	$L_2(4217^2), S_4(4217), U_3(4217),$ $U_4(4217)$
4219	23	$L_3(113^2), L_2(113^3), L_2(113^6),$ $S_6(113), S_4(113^3), O_7(113),$ $O_8^+(113), G_2(113), G_2(113^2),$ ${}^3D_4(113), U_3(113), U_4(113)$
4229	5	$L_2(4229^2), S_4(4229)$
4243	12	$U_3(4243)$
4253	11	$L_3(4253), L_2(4253^3), G_2(4253),$ $U_3(4253)$
4261	15	$L_2(4261^2), S_4(4261), U_3(4261),$ $U_4(4261)$
4271	7	$L_5(37), L_6(37), U_5(599),$ $L_3(4271)$
4273	12	$U_3(2663)$
4283	8	$L_3(4283)$
4289	12	$L_2(3761^2), S_4(3761), L_3(4289)$
4297	33	$U_3(2887), U_3(4297)$
4327	13	$L_2(4327^2), S_4(4327)$
4337	5	$L_2(4337^2), S_4(4337)$
4357	11	$U_3(1319), U_4(1319), L_2(4357^2),$ $S_4(4357)$

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p	$ \mathfrak{S}_p $	G
4363	15	$L_2(4363^2), S_4(4363), U_3(4363),$ $U_4(4363)$
4373	21	$L_2(4373^2), S_4(4373)$
4391	9	$L_2(4391^2), S_4(4391)$
4421	5	$L_2(3469^2), S_4(3469)$
4423	31	$L_3(67^2), L_2(67^3), S_6(67),$ $O_7(67), O_8^+(67), G_2(67),$ $U_3(67), U_4(67), U_3(4357),$ $U_4(4357), L_2(4423^2), S_4(4423)$
4441	8	$L_3(3539)$
4457	8	$L_3(4457)$
4481	4	$L_3(4481)$
4483	13	$L_2(4483^2), S_4(4483)$
4493	20	$L_2(2213^2), S_4(2213), U_4(2213),$ $L_2(4493^2), S_4(4493)$
4513	7	$L_2(4513^2), S_4(4513)$
4519	7	$U_3(3463), U_4(3463)$
4523	26	$L_3(4523)$
4549	14	$U_3(4549)$
4561	18	$L_5(27), L_3(3^5), L_6(27), L_4(3^5),$ $L_3(3^{10}), L_2(3^{15}), S_6(3^5),$ $O_7(3^5), O_8^+(3^5), G_2(3^5),$ $L_3(4561)$
4567	19	$L_2(4567^2), S_4(4567)$
4591	9	$U_3(311), U_4(311)$
4597	10	$L_2(2129^2), S_4(2129), L_3(4219)$
4603	29	$L_3(179), L_4(179), L_3(179^2),$ $L_2(179^3), S_6(179), O_7(179),$ $O_8^+(179), G_2(179), L_3(4423),$ $L_4(4423)$
4621	22	$L_3(2857), L_3(4621), L_2(4621^3),$ $G_2(4621), U_3(4621)$
4637	6	$L_2(2593^2), S_4(2593), L_3(4637)$
4639	6	$U_3(1361)$
4643	11	$L_3(4643), L_4(4643), L_2(4643^2),$ $S_4(4643)$
4649	7	$L_2(2803^2), S_4(2803), L_2(4649^2),$ $S_4(4649)$
4651	16	$L_3(787^2), L_2(787^3), S_6(787),$ $O_7(787), O_8^+(787), G_2(787),$ $U_3(787), U_4(787), L_3(4651)$
4657	9	$L_3(967), L_3(4657)$

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p	$ \mathfrak{S}_p $	G	p	$ \mathfrak{S}_p $	G
4673	9	$L_2(1993^2), S_4(1993)$	4967	7	$L_2(4967^2), S_4(4967), U_3(4967), U_4(4967)$
4679	17	$L_2(4679^2), S_4(4679), U_3(4679), U_4(4679)$	4969	12	$L_2(4783^3), G_2(4783), U_3(4783), L_3(4969), L_4(4969), L_2(4969^2), S_4(4969)$
4691	16	$L_7(59), L_8(59), L_3(4691)$	4973	19	$L_2(223^2), S_4(223), U_4(223), U_3(4973)$
4721	7	$L_2(1697^2), S_4(1697), U_4(1697), U_3(1697^2)$	4987	12	$U_3(3851), L_2(4987^2), S_4(4987), U_3(4987), U_4(4987)$
4723	8	$U_3(4723)$	5009	4	$U_3(5009)$
4729	7	$U_3(2693), L_3(4729)$	5023	22	$L_3(953), L_2(953^3), G_2(953), L_2(5023^2), S_4(5023)$
4733	31	$L_7(7), L_8(7), L_9(7), L_{10}(7), L_7(49), L_2(7^7), S_{14}(7), O_{15}(7), O_{14}^+(7), O_{16}^+(7), L_2(4733^2), S_4(4733)$	5051	10	$L_3(5051)$
4751	11	$L_2(4751^2), S_4(4751)$	5059	28	$L_3(1913^2), L_2(1913^3), S_6(1913), O_7(1913), O_8^+(1913), G_2(1913), U_3(1913), U_4(1913), U_3(5059)$
4783	7	$L_3(3037), L_3(4783)$	5077	12	$L_4(4219), L_2(4219^2), S_4(4219), L_3(5077), L_2(5077^3), G_2(5077), U_3(5077)$
4787	5	$L_2(4787^2), S_4(4787)$	5087	15	$L_2(5087^2), S_4(5087)$
4789	12	$L_2(1481^2), S_4(1481), L_3(3109), L_2(4789^2), S_4(4789), U_3(4789), U_4(4789)$	5099	7	$L_3(5099), L_4(5099), L_2(5099^2), S_4(5099)$
4793	10	$L_4(3313), L_2(3313^2), S_4(3313)$	5101	11	$L_2(101^2), S_4(101), U_4(101), L_3(5101)$
4799	4	$L_3(4799)$	5107	15	$L_3(311), L_4(311), L_3(311^2), L_2(311^3), S_6(311), O_7(311), O_8^+(311), G_2(311)$
4801	14	$U_3(2341)$	5113	21	$L_3(71), L_4(71), L_5(71), L_6(71), L_3(71^2), L_2(71^3), S_6(71), O_7(71), O_8^+(71), G_2(71), L_2(5113^2), S_4(5113), U_3(5113), U_4(5113)$
4813	7	$U_3(1889), U_4(1889)$	5119	33	$L_2(5119^2), S_4(5119), U_3(5119), U_4(5119)$
4817	20	$L_4(1291), L_2(1291^2), S_4(1291), L_2(4817^2), S_4(4817)$	5153	27	$L_4(227), L_2(227^2), L_3(227^2), S_4(227), S_6(227), O_7(227), O_8^+(227), U_4(227), L_2(5153^2), S_4(5153), U_3(5153), U_4(5153)$
4831	33	$L_2(4831^2), S_4(4831)$	5167	18	$L_6(5^3), L_3(5^6), L_2(5^9), S_6(5^3), O_7(5^3), O_8^+(5^3), G_2(5^3), {}^2E_6(5), U_9(5), U_3(5^3), U_{10}(5), U_4(5^3), U_3(5167)$
4861	12	$L_3(4861)$	5171	11	$L_2(5171^2), S_4(5171)$
4877	21	$L_4(719), L_2(719^2), L_3(719^2), S_4(719), S_6(719), O_7(719), O_8^+(719), U_4(719)$	5189	10	$U_3(5189)$
4889	17	$L_2(4159^2), S_4(4159)$			
4903	13	$U_3(2417), U_4(2417), L_3(4903), L_2(4903^3), G_2(4903), U_3(4903)$			
4909	14	$L_2(1613^2), S_4(1613), L_3(4909)$			
4933	15	$L_3(2131), L_3(2801), L_4(2801), L_4(3739), L_2(3739^2), S_4(3739), L_3(4933), L_4(4933), L_2(4933^2), S_4(4933)$			
4937	9	$L_2(4937^2), S_4(4937)$			
4951	13	$L_3(2689), L_4(2689), L_3(4951), L_2(4951^3), G_2(4951), U_3(4951)$			
4957	16	$L_4(359), L_2(359^2), S_4(359), L_2(4957^2), S_4(4957)$			

continued

continued

p	$ \mathfrak{S}_p $	G
5197	23	$U_3(1879), L_3(3319^2), L_2(3319^3), S_6(3319), O_7(3319), O_8^+(3319), G_2(3319), U_3(3319), U_4(3319), U_3(5197)$
5209	20	$U_3(1193)$
5227	7	$L_2(5227^2), S_4(5227)$
5231	5	$L_5(307), L_6(307)$
5233	7	$L_3(331), L_4(331)$
5237	26	$U_3(5237)$
5261	17	$L_2(827^2), S_4(827), U_4(827), L_3(5261)$
5281	21	$U_{11}(5), U_{12}(5), L_3(3877), U_3(5281)$
5323	21	$L_3(1283^2), L_2(1283^3), S_6(1283), O_7(1283), O_8^+(1283), G_2(1283), U_3(1283), U_4(1283), L_2(5323^2), S_4(5323)$
5347	9	$L_3(479), L_4(479), L_2(5347^2), S_4(5347)$
5351	32	$U_3(5351)$
5381	8	$L_3(5381)$
5413	7	$L_2(5413^2), S_4(5413)$
5419	38	$L_7(64), L_3(2^{14}), L_2(2^{21}), L_8(64), S_{14}(8), S_6(2^7), S_{16}(8), O_{16}^+(8), O_8^+(2^7), O_{14}^-(8), O_{16}^-(8), G_2(2^7), U_7(8), U_3(2^7), U_8(8), U_4(2^7), L_3(127), L_4(127), L_3(127^2), L_2(127^3), S_6(127), O_7(127), O_8^+(127), G_2(127), L_3(5419)$
5431	8	$U_3(5431)$
5437	6	$L_3(5437)$
5441	7	$L_3(5441), L_2(5441^3), G_2(5441), U_3(5441)$
5443	9	$L_2(5443^2), S_4(5443)$
5477	7	$L_2(5477^2), S_4(5477), U_3(5477), U_4(5477)$
5479	11	$U_3(2777), U_4(2777), L_3(5479), L_4(5479), L_2(5479^2), S_4(5479)$
5483	23	$L_3(5483), L_2(5483^3), G_2(5483), U_3(5483)$

continued

p	$ \mathfrak{S}_p $	G
5503	12	$L_3(929), L_2(929^3), G_2(929), L_2(5503^2), S_4(5503), U_3(5503), U_4(5503)$
5507	17	$L_2(5507^2), S_4(5507), U_3(5507), U_4(5507)$
5527	11	$L_2(877^3), G_2(877), U_3(877), L_2(4651^3), G_2(4651), U_3(4651)$
5531	30	$O_{10}^-(239), U_5(239), U_6(239)$
5557	14	$L_2(3079^2), S_4(3079), U_4(3079), L_2(5557^2), S_4(5557), U_3(5557), U_4(5557)$
5569	8	$L_2(2243^3), G_2(2243), U_3(2243)$
5573	12	$L_4(2017), L_2(2017^2), S_4(2017)$
5581	19	$L_5(53), L_6(53), L_2(53^5), U_3(2459), L_3(5581), L_4(5581), L_2(5581^2), S_4(5581)$
5591	34	$U_3(5591)$
5623	19	$L_2(5623^2), S_4(5623)$
5639	4	$L_3(5639)$
5641	17	$L_4(1429), L_2(1429^2), L_3(1429^2), S_4(1429), S_6(1429), O_7(1429), O_8^+(1429), U_4(1429), L_2(5641^2), S_4(5641)$
5647	14	$L_3(853), L_4(853), L_3(853^2), L_2(853^3), S_6(853), O_7(853), O_8^+(853), G_2(853), L_3(4793)$
5653	6	$U_3(17^3)$
5657	4	$U_3(5657)$
5659	15	$L_3(5659), L_2(5659^3), G_2(5659), U_3(5659)$
5683	8	$U_3(5683)$
5693	13	$L_2(1193^2), S_4(1193), U_4(1193), U_3(5693)$
5701	13	$L_2(5701^2), S_4(5701)$
5711	8	$L_3(5711)$
5717	23	$L_2(3301^2), S_4(3301)$
5743	11	$L_3(5743), L_4(5743), L_2(5743^2), S_4(5743)$
5749	44	$L_3(331^2), L_2(331^3), S_6(331), O_7(331), O_8^+(331), G_2(331), U_3(331), U_4(331), L_2(4943^2), S_4(4943), L_2(5419^3), G_2(5419), U_3(5419)$

continued

p	$ \mathfrak{S}_p $	G	p	$ \mathfrak{S}_p $	G
5779	8	$L_3(2851), L_3(2927), L_3(5779)$	6079	20	$L_3(1553), L_4(1553), L_3(1553^2),$ $L_2(1553^3), S_6(1553), O_7(1553),$ $O_8^+(1553), G_2(1553), L_3(6079)$
5791	20	$L_3(4219^2), L_2(4219^3), S_6(4219),$ $O_7(4219), O_8^+(4219), G_2(4219),$ $U_3(4219), U_4(4219), L_3(5791)$	6089	5	$L_2(6089^2), S_4(6089)$
5801	8	$L_3(5801)$	6091	14	$U_3(5347), U_4(5347), L_3(6091)$
5807	11	$L_3(5807), L_4(5807), L_2(5807^2),$ $S_4(5807)$	6121	27	$L_3(1153^2), L_2(1153^3), S_6(1153),$ $O_7(1153), O_8^+(1153), G_2(1153),$ $U_3(1153), U_4(1153), L_3(4969^2),$ $L_2(4969^3), S_6(4969), O_7(4969),$ $O_8^+(4969), G_2(4969), U_3(4969),$ $U_4(4969)$
5813	11	$L_2(5813^2), S_4(5813)$	6133	15	$L_3(6133), L_4(6133), L_2(6133^2),$ $S_4(6133)$
5821	11	$L_2(3673^3), G_2(3673), U_3(3673),$ $L_3(5821)$	6143	11	$L_2(6143^2), S_4(6143)$
5827	17	$L_3(5827), L_2(5827^3), G_2(5827),$ $U_3(5827)$	6151	15	$L_2(6151^2), S_4(6151)$
5843	9	$L_2(5843^2), S_4(5843)$	6163	28	$L_3(79^2), L_2(79^3), L_4(79^2),$ $S_6(79), S_8(79), O_7(79), O_9(79),$ $O_8^+(79), O_8^-(79), O_{10}^-(79),$ $G_2(79), U_3(79), U_4(79), U_5(79),$ $U_6(79), L_2(6163^2), S_4(6163)$
5849	4	$U_3(5849)$	6173	29	$L_2(2447^2), S_4(2447), L_2(6173^2),$ $S_4(6173)$
5851	16	$L_3(577), L_4(577), L_3(577^2),$ $L_2(577^3), S_6(577), O_7(577),$ $O_8^+(577), G_2(577), L_3(5273)$	6197	5	$L_2(6197^2), S_4(6197)$
5857	8	$L_2(4547^2), S_4(4547), U_3(5857)$	6211	22	$L_3(137^2), L_2(137^3), L_4(137^2),$ $S_6(137), S_8(137), O_7(137),$ $O_9(137), O_8^+(137), O_8^-(137),$ $O_{10}^-(137), G_2(137), U_3(137),$ $U_4(137), U_5(137), U_6(137)$
5861	10	$L_2(5107^2), S_4(5107), L_3(5861)$	6217	10	$L_3(2459), L_2(2459^3), G_2(2459),$ $L_2(6217^2), S_4(6217)$
5867	5	$L_2(5867^2), S_4(5867)$	6229	23	$L_4(1451), L_2(1451^2), S_4(1451),$ $L_3(6229)$
5869	15	$L_3(5869), L_4(5869), L_2(5869^2),$ $S_4(5869)$	6247	14	$U_3(3931), L_2(6247^2), S_4(6247)$
5879	4	$U_3(5879)$	6257	11	$L_2(4673^2), S_4(4673), L_2(6257^2),$ $S_4(6257)$
5881	28	$L_2(277^3), G_2(277), U_3(277),$ $L_4(4783), L_2(4783^2), L_3(4783^2),$ $S_4(4783), S_6(4783), O_7(4783),$ $O_8^+(4783), U_4(4783)$	6263	9	$L_2(6263^2), S_4(6263)$
5923	7	$L_2(5923^2), S_4(5923)$	6269	9	$L_2(1523^2), S_4(1523), L_3(6269),$ $L_4(6269), L_2(6269^2), S_4(6269)$
5927	14	$U_3(5927)$	6277	25	$L_4(1033), L_2(1033^2), L_3(1033^2),$ $S_4(1033), S_6(1033), O_7(1033),$ $O_8^+(1033), U_4(1033), U_3(2309),$ $U_4(2309), L_3(6277), L_4(6277),$ $L_2(6277^2), S_4(6277)$
6007	7	$L_2(6007^2), S_4(6007)$			
6029	12	$L_2(1801^2), S_4(1801), U_3(6029)$			
6037	16	$L_3(509), L_4(509), L_3(509^2),$ $L_2(509^3), S_6(509), O_7(509),$ $O_8^+(509), G_2(509), L_3(5527)$			
6043	9	$L_3(4327), L_4(4327), L_2(6043^2),$ $S_4(6043)$			
6053	18	$L_2(3221^2), S_4(3221), U_4(3221)$			
6067	11	$L_3(6067), L_4(6067), L_2(6067^2),$ $S_4(6067)$			
6073	8	$U_3(4231)$			

continued

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p	$ \mathfrak{S}_p $	G	p	$ \mathfrak{S}_p $	G
6287	17	$L_3(6287), L_2(6287^3), G_2(6287), U_3(6287)$	6529	32	$L_3(491), L_4(491), L_3(491^2), L_2(491^3), S_6(491), O_7(491), O_8^+(491), G_2(491), L_4(2311), L_2(2311^2), S_4(2311), L_3(6037), U_3(6529)$
6299	4	$U_3(6299)$	6547	8	$U_3(2333), U_4(2333), U_3(6547)$
6301	19	$L_3(3323), L_4(3323), L_3(3323^2), L_2(3323^3), S_6(3323), O_7(3323), O_8^+(3323), G_2(3323)$	6551	5	$L_2(6551^2), S_4(6551)$
6311	9	$L_2(6311^2), S_4(6311)$	6553	13	$L_2(6553^2), S_4(6553)$
6317	8	$L_3(6317)$	6569	5	$L_2(6569^2), S_4(6569)$
6323	11	$L_3(6323), L_4(6323), L_2(6323^2), S_4(6323)$	6571	9	$L_2(6571^2), S_4(6571)$
6337	9	$L_2(6337^2), S_4(6337)$	6577	13	$L_3(353), L_4(353), L_3(353^2), L_2(353^3), S_6(353), O_7(353), O_8^+(353), G_2(353)$
6343	13	$L_3(557), L_4(557)$	6581	20	$L_3(6581)$
6353	11	$L_3(6353), L_4(6353), L_2(6353^2), S_4(6353)$	6607	14	$L_3(6607)$
6359	4	$U_3(6359)$	6619	20	$L_3(569)$
6367	8	$L_3(769)$	6637	18	$L_3(6637)$
6373	11	$L_2(1879^2), S_4(1879), U_4(1879), L_3(5749)$	6659	4	$L_3(6659)$
6379	19	$L_3(3373^2), L_2(3373^3), S_6(3373), O_7(3373), O_8^+(3373), G_2(3373), U_3(3373), U_4(3373)$	6661	15	$L_2(6661^2), S_4(6661)$
6389	12	$L_2(4297^2), S_4(4297), U_4(4297)$	6673	10	$L_2(2437^2), S_4(2437), L_3(5279)$
6397	27	$L_2(6397^2), S_4(6397)$	6679	12	$U_3(5737)$
6421	8	$L_3(6421)$	6691	13	$L_2(6691^2), S_4(6691)$
6427	24	$L_3(6427)$	6701	7	$L_4(1721), L_2(1721^2), S_4(1721), L_3(6701)$
6449	4	$L_3(6449)$	6703	10	$U_3(1481), U_4(1481), L_3(6703)$
6451	21	$L_2(6451^2), S_4(6451)$	6733	13	$L_3(619), L_2(619^3), G_2(619), L_3(6113), L_3(6733), L_2(6733^3), G_2(6733), U_3(6733)$
6469	8	$U_3(4993), L_2(6469^2), S_4(6469)$	6737	34	$L_4(2393), L_2(2393^2), L_3(2393^2), S_4(2393), S_6(2393), O_7(2393), O_8^+(2393), U_4(2393), L_3(6737)$
6473	10	$U_3(6473)$	6763	18	$L_3(6763)$
6481	50	$L_{12}(9), L_6(3^4), L_4(3^6), L_3(3^8), L_2(3^{12}), L_5(3^6), L_2(3^{24}), S_{24}(3), S_{12}(9), S_8(27), S_6(3^4), S_4(3^6), S_{10}(27), S_4(3^{12}), O_{25}(3), O_{13}(9), O_9(27), O_7(3^4), O_{11}(27), O_{14}^+(9), O_{10}^+(27), O_8^+(3^4), O_{12}^+(27), O_8^-(27), O_{12}^-(9), O_{24}^-(3), O_{10}^-(27), G_2(3^4), G_2(3^8), F_4(9), E_6(9), E_8(3), {}^3D_4(9), {}^3D_4(3^4), U_3(3^4), U_4(3^4), U_8(27), L_2(6481^2), S_4(6481)$	6779	4	$U_3(6779)$
6491	32	$U_3(6491)$	6781	14	$L_2(2927^3), G_2(2927), U_3(2927)$
6521	13	$L_2(4157^2), S_4(4157), L_2(6521^2), S_4(6521)$	6793	15	$L_2(709^2), S_4(709), U_4(709), L_3(6793)$
			6803	25	$L_3(6803), L_2(6803^3), G_2(6803), U_3(6803)$
			6823	6	$U_3(6823)$
			6827	5	$L_2(6827^2), S_4(6827)$
			6829	8	$L_2(5233^2), S_4(5233), L_3(6829)$

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p	$ \mathfrak{S}_p $	G	p	$ \mathfrak{S}_p $	G
6833	11	$L_2(1307^2), S_4(1307)$	7177	20	$L_3(2039^2), L_2(2039^3), S_6(2039),$ $O_7(2039), O_8^+(2039), G_2(2039),$ $U_3(2039), U_4(2039), L_3(7177)$
6841	23	$L_2(53^6), S_4(53^3), G_2(53^2),$ ${}^3D_4(53), U_3(53^2), L_3(6841)$	7187	11	$L_3(7187), L_4(7187), L_2(7187^2),$ $S_4(7187)$
6863	19	$L_3(6863), L_4(6863), L_2(6863^2),$ $L_3(6863^2), L_2(6863^3), S_4(6863),$ $S_6(6863), O_7(6863), O_8^+(6863),$ $G_2(6863), U_3(6863), U_4(6863)$	7193	22	$L_4(967), L_2(967^2), S_4(967),$ $L_3(7193), L_4(7193), L_2(7193^2),$ $S_4(7193)$
6871	14	$L_3(6871)$	7207	9	$L_2(7207^2), S_4(7207), U_3(7207),$ $U_4(7207)$
6899	10	$L_3(6899)$	7213	16	$L_4(1999), L_2(1999^2), L_3(1999^2),$ $S_4(1999), S_6(1999), O_7(1999),$ $O_8^+(1999), U_4(1999), U_3(7213)$
6907	12	$L_2(5051^3), G_2(5051), U_3(5051),$ $L_3(6907), L_2(6907^3), G_2(6907),$ $U_3(6907)$	7219	13	$L_3(4493), L_4(4493)$
6911	9	$L_2(6911^2), S_4(6911)$	7237	11	$L_2(1831^3), G_2(1831), U_3(1831),$ $U_3(5407)$
6917	41	$L_4(263), L_2(263^2), L_3(263^2),$ $S_4(263), S_6(263), O_7(263),$ $O_8^+(263), U_4(263), L_2(6917^2),$ $S_4(6917)$	7253	33	$L_2(7253^2), S_4(7253)$
6949	12	$U_3(6949)$	7283	16	$L_3(7283)$
6959	5	$L_2(6959^2), S_4(6959)$	7297	15	$L_3(3761), L_4(3761), L_2(7297^2),$ $S_4(7297)$
6961	9	$U_3(727^2), L_3(6961)$	7307	5	$L_2(7307^2), S_4(7307)$
6967	7	$U_3(383), U_3(6967)$	7309	14	$U_3(7309)$
6971	8	$L_3(6971)$	7321	25	$L_4(11^2), L_2(11^4), L_3(11^4),$ $S_8(11), S_4(11^2), S_6(11^2),$ $O_9(11), O_7(11^2), O_{10}^+(11),$ $O_8^+(11^2), O_8^-(11), F_4(11),$ $U_4(11^2), U_3(7013)$
6977	11	$L_2(2063^2), S_4(2063), L_2(6977^2),$ $S_4(6977)$	7333	23	$L_2(2909^2), S_4(2909), U_4(2909),$ $L_2(4271^3), G_2(4271), U_3(4271)$
6983	13	$L_2(6983^2), S_4(6983), U_3(6983),$ $U_4(6983)$	7351	28	$L_6(149), L_3(149^2), L_2(149^3),$ $S_6(149), O_7(149), O_8^+(149),$ $G_2(149), U_3(149), U_4(149)$
6991	8	$L_3(1381)$	7369	33	$L_2(607^2), S_4(607), L_4(3373^2),$ $L_2(3373^4), S_8(3373), S_4(3373^2),$ $O_9(3373), O_8^-(3373)$
6997	7	$U_3(2909), L_3(6997)$	7433	22	$L_2(983^2), S_4(983), U_4(983)$
7027	22	$L_3(523), L_4(523), L_3(523^2),$ $L_2(523^3), S_6(523), O_7(523),$ $O_8^+(523), G_2(523), U_6(523)$	7459	27	$L_3(229^2), L_2(229^3), S_6(229),$ $O_7(229), O_8^+(229), G_2(229),$ $U_3(229), U_4(229)$
7039	8	$L_2(6737^3), G_2(6737), U_3(6737)$	7477	7	$U_3(3469), U_4(3469)$
7057	16	$L_3(6911), L_4(6911), U_3(7057)$	7481	9	$L_2(6073^2), S_4(6073)$
7079	27	$L_2(7079^2), S_4(7079)$	7489	13	$L_3(2467), L_3(5021)$
7103	12	$L_2(7103^2), S_4(7103), U_3(7103),$ $U_4(7103), U_5(7103)$	7499	10	$L_3(7499)$
7121	10	$L_2(6343^2), S_4(6343), L_3(7121)$			
7127	5	$L_2(7127^2), S_4(7127)$			
7129	27	$L_3(1249), L_3(5879), L_2(5879^3),$ $G_2(5879)$			
7151	10	$L_3(7151)$			
7159	20	$L_3(7159)$			

continued

continued

p	$ \mathfrak{S}_p $	G
7507	14	$U_3(607), U_4(607), U_3(7507)$
7529	13	$L_3(7529), L_2(7529^3), G_2(7529), U_3(7529)$
7537	9	$L_4(1049), L_2(1049^2), S_4(1049), L_3(7537)$
7549	21	$L_2(23^6), S_4(23^3), G_2(23^2), {}^3D_4(23), U_3(23^2), U_4(23^3), L_2(7549^2), S_4(7549), U_3(7549), U_4(7549)$
7559	4	$L_3(7559)$
7561	15	$U_3(6263), U_4(6263)$
7577	11	$L_4(6037), L_2(6037^2), S_4(6037), L_3(7577)$
7583	8	$U_3(7583)$
7603	9	$L_2(7603^2), S_4(7603), U_3(7603), U_4(7603)$
7607	19	$L_2(7607^2), S_4(7607), U_3(7607), U_4(7607)$
7621	26	$L_2(5^{15}), G_2(5^5), U_5(5^3), U_3(5^5), U_6(5^3), U_7(5^3), L_3(7621)$
7639	10	$L_3(4663), L_3(7639), L_4(7639), L_2(7639^2), S_4(7639)$
7649	23	$L_2(7649^2), S_4(7649)$
7669	9	$L_2(7669^2), S_4(7669), U_3(7669), U_4(7669)$
7673	19	$L_4(277), L_2(277^2), L_3(277^2), S_4(277), S_6(277), O_7(277), O_8^+(277), U_4(277), U_5(277), U_6(277)$
7681	11	$L_2(6997^3), G_2(6997), U_3(6997), U_3(7681)$
7687	8	$U_3(5413), U_4(5413), L_3(7687)$
7699	10	$L_3(2269), L_2(7699^2), S_4(7699), U_3(7699), U_4(7699)$
7703	16	$L_3(7703)$
7717	10	$L_2(2953^2), S_4(2953), U_4(2953)$
7723	6	$U_3(7723)$
7727	16	$L_3(7727)$
7753	6	$L_3(7349)$
7759	35	$L_3(1759), L_2(1759^3), G_2(1759), U_3(7759)$

continued

p	$ \mathfrak{S}_p $	G
7789	15	$L_3(233), L_4(233), L_3(233^2), L_2(233^3), S_6(233), O_7(233), O_8^+(233), G_2(233), L_2(7789^2), S_4(7789)$
7841	17	$L_2(7643^2), S_4(7643), L_2(7841^2), S_4(7841)$
7853	23	$L_4(1759), L_2(1759^2), L_3(1759^2), S_4(1759), S_6(1759), O_7(1759), O_8^+(1759), U_4(1759)$
7867	9	$L_2(7867^2), S_4(7867)$
7873	8	$L_4(4283), L_2(4283^2), S_4(4283)$
7877	4	$U_3(7877)$
7879	9	$L_2(1367^3), G_2(1367), U_3(1367), L_3(7879)$
7883	23	$L_2(7883^2), S_4(7883), U_3(7883), U_4(7883)$
7907	14	$L_3(7907)$
7919	10	$U_3(7919)$
7927	9	$L_2(7927^2), S_4(7927)$
7933	8	$L_3(5927), L_2(5927^3), G_2(5927)$
7949	4	$U_3(7949)$
7963	33	$L_2(7963^2), S_4(7963)$
7993	18	$U_3(7993)$
8009	11	$L_4(283), L_2(283^2), L_3(283^2), S_4(283), S_6(283), O_7(283), O_8^+(283), U_4(283)$
8011	22	$L_3(89), L_4(89), L_5(89), L_6(89), L_3(89^2), L_2(89^3), L_2(89^6), S_6(89), S_4(89^3), O_7(89), O_8^+(89), G_2(89), G_2(89^2), {}^3D_4(89), U_3(8011)$
8039	27	$L_3(8039), L_4(8039), L_2(8039^2), L_3(8039^2), L_2(8039^3), S_4(8039), S_6(8039), O_7(8039), O_8^+(8039), G_2(8039), U_3(8039), U_4(8039)$
8069	14	$U_3(8069)$
8089	8	$L_4(2293), L_2(2293^2), S_4(2293)$
8093	13	$L_2(8093^2), S_4(8093), U_3(8093), U_4(8093)$
8101	15	$L_2(8011^2), S_4(8011), U_4(8011), L_3(8101)$
8111	8	$U_3(8111)$

continued

p	$ \mathfrak{S}_p $	G	p	$ \mathfrak{S}_p $	G
8117	11	$L_2(1733^2), S_4(1733), L_2(8117^2), S_4(8117)$	8389	37	$L_3(691), L_4(691), L_2(3449^2), S_4(3449), U_4(3449), L_3(8389)$
8147	16	$L_3(8147)$	8423	9	$L_2(8423^2), S_4(8423)$
8161	13	$L_3(2903), L_4(2903), L_2(8161^2), S_4(8161), U_3(8161), U_4(8161)$	8429	7	$L_3(8429), L_2(8429^3), G_2(8429), U_3(8429)$
8179	15	$U_3(1097), U_3(8179)$	8443	7	$L_2(8443^2), S_4(8443)$
8191	44	$L_{13}(2), L_{14}(2), L_{15}(2), L_{16}(2), L_{13}(4), L_2(2^{13}), L_{14}(4), L_{15}(4), L_2(2^{26}), S_{26}(2), S_{28}(2), S_{30}(2), S_4(2^{13}), O_{26}^+(2), O_{28}^+(2), O_{30}^+(2), O_{32}^+(2), O_{28}^-(2), O_{30}^-(2), L_2(8101^3), G_2(8101), U_3(8101), L_2(8191^2), S_4(8191), S_z(2^{13})$	8447	16	$U_3(8447)$
8209	17	$L_3(3^9), L_2(2383^4), S_4(2383^2), L_3(4943), L_4(4943), L_3(8209)$	8461	10	$U_3(1777), U_4(1777), U_3(8461)$
8219	4	$L_3(8219)$	8501	17	$L_4(4481), L_2(4481^2), S_4(4481), U_3(8501)$
8221	15	$L_2(8221^2), S_4(8221), U_3(8221), U_4(8221)$	8521	9	$L_2(8521^2), S_4(8521)$
8237	9	$L_2(8237^2), S_4(8237)$	8527	12	$U_3(8527)$
8243	22	$L_3(8243)$	8537	7	$L_2(8537^2), S_4(8537), U_3(8537), U_4(8537)$
8263	9	$U_3(241), U_4(241)$	8539	6	$U_3(5987)$
8269	19	$L_3(157), L_4(157), L_3(157^2), L_2(157^3), S_6(157), O_7(157), O_8^+(157), G_2(157), L_4(643), L_2(643^2), S_4(643), L_3(8111), L_2(8111^3), G_2(8111)$	8563	12	$L_3(8563)$
8273	16	$U_3(8273)$	8573	13	$L_3(8573), L_4(8573), L_2(8573^2), S_4(8573)$
8287	9	$L_2(569^3), G_2(569), U_3(569), U_3(8287)$	8581	22	$L_2(131^2), S_4(131), U_4(131), L_2(8581^2), S_4(8581)$
8291	7	$L_3(8291), L_2(8291^3), G_2(8291), U_3(8291)$	8597	5	$L_2(8597^2), S_4(8597)$
8297	27	$L_3(8297), L_4(8297), L_2(8297^2), L_3(8297^2), L_2(8297^3), S_4(8297), S_6(8297), O_7(8297), O_8^+(8297), G_2(8297), U_3(8297), U_4(8297)$	8599	12	$L_3(7393)$
8317	15	$L_2(8317^2), S_4(8317)$	8609	18	$L_2(6779^2), S_4(6779), U_4(6779)$
8329	26	$L_3(8329)$	8623	6	$U_3(8623)$
8363	11	$L_2(8363^2), S_4(8363), U_3(8363), U_4(8363)$	8629	17	$U_3(3307), U_4(3307), U_3(5323), U_4(5323)$
8369	12	$L_4(7703), L_2(7703^2), S_4(7703)$	8641	11	$L_2(1583^2), S_4(1583), U_4(1583), U_3(8641)$
8377	13	$L_2(8377^2), S_4(8377)$	8647	19	$U_3(7853), L_3(8647)$
8387	5	$L_2(8387^2), S_4(8387)$	8663	9	$L_2(8663^2), S_4(8663)$
			8669	16	$L_4(4793), L_2(4793^2), S_4(4793), L_2(8669^2), S_4(8669), U_3(8669), U_4(8669)$
			8681	11	$L_2(3911^2), S_4(3911)$
			8689	7	$L_2(8689^2), S_4(8689)$
			8707	11	$L_2(8707^2), S_4(8707), U_3(8707), U_4(8707)$
			8713	8	$L_3(8713)$
			8719	14	$L_3(2281)$
			8731	9	$U_3(3659), U_4(3659)$

continued

continued

p	$ \mathfrak{S}_p $	G
8737	11	$L_2(2269^3), G_2(2269), U_3(2269), U_3(6469), U_4(6469), U_3(8737)$
8747	8	$L_3(8747)$
8761	24	$L_3(1733), L_4(1733), L_3(7027), L_2(8293^2), S_4(8293)$
8779	9	$L_3(8779), L_2(8779^3), G_2(8779), U_3(8779)$
8783	23	$L_2(8783^2), S_4(8783)$
8807	15	$L_2(8807^2), S_4(8807)$
8821	15	$U_3(467^2), U_3(2437), U_4(2437), U_3(8821)$
8831	8	$U_3(8831)$
8837	4	$U_3(8837)$
8839	13	$U_3(4373), U_4(4373)$
8861	7	$L_2(8861^2), S_4(8861), U_3(8861), U_4(8861)$
8863	6	$U_3(8863)$
8867	22	$U_3(8867)$
8887	9	$L_2(8887^2), S_4(8887)$
8893	35	$L_4(2851), L_2(2851^2), S_4(2851), U_3(8893)$
8923	8	$L_3(3847)$
8929	6	$L_3(4339)$
8933	11	$L_2(8171^2), S_4(8171)$
8941	15	$L_4(5861), L_2(5861^2), S_4(5861), L_3(8941)$
8951	17	$L_3(8951), L_2(8951^3), G_2(8951), U_3(8951)$
8971	31	$L_3(8629), U_3(8971)$
8999	7	$L_2(8999^2), S_4(8999), U_3(8999), U_4(8999)$
9001	11	$L_4(1237), L_2(1237^2), S_4(1237), L_3(9001)$
9007	6	$L_3(9007)$
9011	5	$L_2(9011^2), S_4(9011)$
9043	9	$L_2(9043^2), S_4(9043)$
9049	14	$L_4(7687), L_2(7687^2), S_4(7687)$
9067	29	$L_3(9067), L_4(9067), L_2(9067^2), S_4(9067)$

continued

p	$ \mathfrak{S}_p $	G
9091	22	$L_3(3389^2), L_2(3389^3), S_6(3389), O_7(3389), O_8^+(3389), G_2(3389), U_3(3389), U_4(3389), L_3(9091)$
9103	14	$L_3(4723), L_2(4723^3), G_2(4723), L_3(9103), L_2(9103^3), G_2(9103), U_3(9103)$
9109	24	$U_3(3121), L_3(9109), L_2(9109^3), G_2(9109), U_3(9109)$
9127	9	$U_3(3011), U_4(3011)$
9133	8	$L_3(3797), L_2(9133^2), S_4(9133)$
9157	8	$L_2(2203^2), S_4(2203), U_4(2203)$
9161	23	$L_4(5^5), L_2(5^{10}), L_3(5^{10}), S_4(5^5), S_6(5^5), O_7(5^5), O_8^+(5^5), U_5(25), U_6(25), U_4(5^5)$
9173	12	$L_4(6659), L_2(6659^2), S_4(6659)$
9181	13	$L_3(1009), L_2(1009^3), G_2(1009), L_3(8171), L_4(8171), L_3(9181)$
9187	14	$U_3(9187)$
9199	9	$L_3(3767), L_3(5431), L_2(5431^3), G_2(5431)$
9209	18	$L_2(8863^2), S_4(8863), U_4(8863), L_2(9209^2), S_4(9209)$
9221	9	$L_2(9221^2), S_4(9221)$
9227	14	$L_3(9227)$
9239	4	$U_3(9239)$
9241	20	$U_3(167), U_4(167), L_3(9241)$
9257	24	$L_2(1097^2), S_4(1097), U_4(1097)$
9277	11	$L_3(601), L_4(601), L_4(8389), L_2(8389^2), S_4(8389), L_3(9277)$
9281	4	$L_3(9281)$
9283	19	$L_3(2843), L_4(2843), L_3(2843^2), L_2(2843^3), S_6(2843), O_7(2843), O_8^+(2843), G_2(2843)$
9337	7	$L_3(4937), L_4(4937)$
9341	6	$L_4(6703), L_2(6703^2), S_4(6703)$
9343	10	$L_2(6113^3), G_2(6113), U_3(6113)$
9349	29	$L_2(73^6), S_4(73^3), G_2(73^2), {}^3D_4(73), U_3(73^2), U_3(4021)$
9377	18	$L_2(6529^2), S_4(6529), U_4(6529)$
9391	15	$L_3(983), L_4(983), L_3(983^2), L_2(983^3), S_6(983), O_7(983), O_8^+(983), G_2(983)$

continued

p	$ \mathfrak{S}_p $	G	p	$ \mathfrak{S}_p $	G
9403	15	$L_3(9403), L_2(9403^3), G_2(9403), U_3(9403)$	9817	26	$L_2(4027^6), S_4(4027^3), G_2(4027^2), {}^3D_4(4027), U_3(4027^2), L_3(8861), L_4(8861), L_3(8861^2), L_2(8861^3), S_6(8861), O_7(8861), O_8^+(8861), G_2(8861)$
9419	4	$L_3(9419)$	9833	11	$L_2(9833^2), S_4(9833), U_3(9833), U_4(9833)$
9421	12	$L_3(9421)$	9839	15	$L_2(9839^2), S_4(9839)$
9431	5	$L_2(9431^2), S_4(9431)$	9851	8	$L_3(9851)$
9433	7	$L_2(8419^2), S_4(8419)$	9859	15	$U_3(4751), U_4(4751)$
9439	25	$L_3(733), L_4(733)$	9871	15	$L_2(9871^2), S_4(9871)$
9461	6	$L_2(7951^2), S_4(7951), U_3(9461)$	9883	6	$L_3(9883)$
9463	15	$L_3(607), L_4(607), L_3(607^2), L_2(607^3), S_6(607), O_7(607), O_8^+(607), G_2(607), L_2(9463^2), S_4(9463)$	9887	19	$L_2(9887^2), S_4(9887), U_3(9887), U_4(9887)$
9467	9	$L_2(9467^2), S_4(9467)$	9901	9	$L_2(9901^2), S_4(9901)$
9479	17	$L_2(9479^2), S_4(9479), U_3(9479), U_4(9479)$	9907	19	$L_3(6571), L_4(6571)$
9491	8	$L_3(9491)$	9923	8	$U_3(9923)$
9511	12	$U_3(3491)$	9929	7	$L_3(9929), L_2(9929^3), G_2(9929), U_3(9929)$
9551	38	$U_3(9551)$	9931	14	$L_3(4231), L_2(4231^3), G_2(4231)$
9587	19	$L_2(9587^2), S_4(9587), U_3(9587), U_4(9587)$	9941	11	$L_2(9941^2), S_4(9941)$
9601	14	$L_3(9601)$	9949	25	$L_2(2543^2), S_4(2543), L_2(9949^2), S_4(9949), U_3(9949), U_4(9949)$
9619	6	$U_3(9619)$	9967	9	$L_3(457), L_4(457)$
9631	17	$L_3(1621), L_4(1621), L_3(8009), U_3(9631)$			
9643	8	$U_3(4597)$			
9649	17	$L_3(9649), L_2(9649^3), G_2(9649), U_3(9649)$			
9661	20	$L_4(139), L_2(139^2), S_4(139)$			
9677	4	$L_3(9677)$			
9679	12	$U_3(9679)$			
9689	11	$L_2(7477^2), S_4(7477)$			
9697	24	$L_3(9697)$			
9721	17	$L_3(9721), L_2(9721^3), G_2(9721), U_3(9721)$			
9733	8	$U_3(9733)$			
9739	12	$L_2(6971^3), G_2(6971), U_3(6971), L_3(9739), L_4(9739), L_2(9739^2), S_4(9739)$			
9791	14	$U_3(9791)$			
9811	13	$U_3(9209), U_4(9209), L_3(9811), L_4(9811), L_2(9811^2), S_4(9811)$			

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